

CLAIMS

What is claimed is:

1. A method of obtaining predictive information for inhomogeneous financial time series, comprising the steps of:
 - 5 electronically receiving financial market transaction data over an electronic network; electronically storing in a computer-readable medium said received financial market transaction data;
 - constructing an inhomogeneous time series z that represents said received financial market transaction data;
 - 10 constructing an exponential moving average operator; constructing an iterated exponential moving average operator based on said exponential moving average operator;
 - constructing a time-translation-invariant, causal operator $\Omega[z]$ that is a convolution operator with kernel ω and that is based on said iterated exponential moving average
 - 15 operator;
 - electronically calculating values of one or more predictive factors relating to said time series z , wherein said one or more predictive factors are defined in terms of said operator $\Omega[z]$; and
 - electronically storing in a computer readable medium said calculated values of one or
 - 20 more predictive factors.

2. The method of claim 1, wherein said operator $\Omega[z]$ has the form:

$$\begin{aligned}
 \Omega[z](t) &= \int_{-\infty}^t dt' \omega(t-t') z(t') \\
 &= \int_0^{\infty} dt' \omega(t') z(t-t').
 \end{aligned}$$

3. The method of claim 1, wherein said exponential moving average operator $\text{EMA}[\tau; z]$ has the form:

$$\text{EMA}[\tau; z](t_n) = \mu \text{EMA}[\tau; z](t_{n-1}) + (v - \mu) z_{n-1} + (1 - v) z_n, \text{ with}$$

$$\begin{aligned}
 \alpha &= \frac{\tau}{t_n - t_{n-1}}, \\
 \mu &= e^{-\alpha},
 \end{aligned}
 \tag{23}$$

where v depends on a chosen interpolation scheme.

4. The method of claim 1, wherein said operator $\Omega[z]$ is a differential operator

5 $\Delta[\tau]$ that has the form:

$$\Delta[\tau] = \gamma(\text{EMA}[\alpha\tau, 1] + \text{EMA}[\alpha\tau, 2] - 2 \text{EMA}[\alpha\beta\tau, 4]),$$

where γ is fixed so that the integral of the kernel of the differential operator from the origin to the first zero is 1; α is fixed by a normalization condition that requires $\Delta[\tau; c] = 0$ for a

10 constant c ; and β is chosen in order to get a short tail for the kernel of the differential operator $\Delta[\tau]$.

5. The method of claim 4 wherein said one or more predictive factors comprises a return of the form $r[\tau] = \Delta[\tau; x]$, where x represents a logarithmic price.

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6. The method of claim 1 wherein said one or more predictive factors comprises a momentum of the form $x - \text{EMA}[\tau; x]$, where x represents a logarithmic price.

7. The method of claim 1 wherein said one or more predictive factors comprises
20 a volatility.

8. The method of claim 7 wherein said volatility is of the form:

$$\text{Volatility}[\tau, \tau', p; z] = \text{MNorm}[\tau/2, p; \Delta[\tau'; z]], \quad \text{where}$$

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$$\text{MNorm}[\tau, p; z] = \text{MA}[\tau; |z|^p]^{1/p}, \quad \text{and}$$

$$\text{MA}[\tau, n] = \frac{1}{n} \sum_{k=1}^n \text{EMA}[\tau', k], \quad \text{with } \tau' = \frac{2\tau}{n+1}, \quad \text{and where } p \text{ satisfies } 0 < p \leq 2,$$

30 and τ' is a time horizon of a return $r[\tau] = \Delta[\tau; x]$, where x represents a logarithmic price.

9. A method of obtaining predictive information for inhomogeneous financial time series, comprising the steps of:

electronically receiving financial market transaction data over an electronic network;
electronically storing in a computer readable medium said received financial market

5 transaction data;

constructing an inhomogeneous time series z that corresponds to said received financial market transaction data;

constructing an exponential moving average operator;

constructing an iterated exponential moving average operator based on said
10 exponential moving average operator;

constructing a time-translation-invariant, causal operator $\Omega[z]$ that is a convolution operator with kernel ω and that is based on said iterated exponential moving average operator;

constructing a standardized time series \hat{z} ;

15 electronically calculating values of one or more predictive factors relating to said time series z , wherein said one or more predictive factors are defined in terms of said standardized time series \hat{z} ; and

electronically storing in a computer readable medium said calculated values of one or more predictive factors.

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10. The method of claim 9 wherein the standardized time series \hat{z} is of the form:

$$\hat{z}[\tau] = \frac{z - \text{MA}[\tau; z]}{\text{MSD}[\tau; z]}, \text{ where}$$

25 $\text{MA}[\tau, n] = \frac{1}{n} \sum_{k=1}^n \text{EMA}[\tau', k], \quad \text{with } \tau' = \frac{2\tau}{n+1}, \quad \text{and}$

$$\text{where } \text{MSD}[\tau, p; z] = \text{MA}[\tau; |z - \text{MA}[\tau; z]|^p]^{1/p}.$$

11. The method of claim 9 wherein said one or more predictive factors comprises
30 a moving skewness.

12. The method of claim 11 wherein said moving skewness is of the form:

MSkewness[$\tau_1, \tau_2; z$] = MA[$\tau_1; \hat{z}[\tau_2]$] where τ_1 is the length of a time interval around

time “now” and τ_2 is the length of a time interval around time “now – τ ”.

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13. The method of claim 12 wherein the standardized time series \hat{z} is of the form:

$$\hat{z}[\tau] = \frac{z - \text{MA}[\tau; z]}{\text{MSD}[\tau; z]}, \text{ where}$$

$$10 \quad \text{MA}[\tau, n] = \frac{1}{n} \sum_{k=1}^n \text{EMA}[\tau', k], \quad \text{with } \tau' = \frac{2\tau}{n+1}, \quad \text{and}$$

$$\text{where } \text{MSD}[\tau, p; z] = \text{MA}[\tau; |z - \text{MA}[\tau; z]|^p]^{1/p}.$$

14. The method of claim 9 wherein said one or more predictive factors comprises

15 a moving kurtosis.

15. The method of claim 14 wherein said moving kurtosis is of the form

$$\text{MKurtosis}[\tau_1, \tau_2; z] = \text{MA}[\tau_1; \hat{z}[\tau_2]^4], \quad \text{where } \tau_1 \text{ is the length of a time interval}$$

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around time “now” and τ_2 is the length of a time interval around time “now – τ .”

16. The method of claim 15 wherein the standardized time series \hat{z} is of the form:

$$25 \quad \hat{z}[\tau] = \frac{z - \text{MA}[\tau; z]}{\text{MSD}[\tau; z]}, \text{ where}$$

$$\text{MA}[\tau, n] = \frac{1}{n} \sum_{k=1}^n \text{EMA}[\tau', k], \quad \text{with } \tau' = \frac{2\tau}{n+1}, \quad \text{and}$$

$$\text{where } \text{MSD}[\tau, p; z] = \text{MA}[\tau; |z - \text{MA}[\tau; z]|^p]^{1/p}.$$

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17. A method of obtaining predictive information for inhomogeneous financial time series, comprising the steps of:

electronically receiving financial market transaction data over an electronic network;
electronically storing in a computer readable medium said received financial market transaction data;

constructing an inhomogeneous time series z that corresponds to said received

5 financial market transaction data;

constructing an exponential moving average operator $\text{EMA}[\tau ; z]$;

constructing an iterated exponential moving average operator based on said

exponential moving average operator $\text{EMA}[\tau ; z]$;

constructing a time-translation-invariant, causal operator $\Omega[z]$ that is a convolution

10 operator with kernel ω and time range τ , and that is based on said iterated exponential moving average operator;

constructing a moving average operator MA that depends on said EMA operator;

constructing a moving standard deviation operator MSD that depends on said MA

operator;

15 electronically calculating values of one or more predictive factors relating to said time series z , wherein said one or more predictive factors depend on one or more of said operators EMA , MA , and MSD ; and

electronically storing in a computer readable medium said calculated values of one or more predictive factors.

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18. The method of claim 17 wherein said one or more predictive factors comprises a moving correlation.

19. The method of claim 18 wherein said moving correlation is of the form:

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$$\text{MCorrelation}[\hat{y}, \hat{z}](t) = \int_0^\infty \int_0^\infty dt' dt'' c(t', t'') \hat{y}(t-t') \hat{z}(t-t'') .$$

20. A method of obtaining predictive information for inhomogeneous financial time series, comprising the steps of:

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electronically receiving financial market transaction data over an electronic network;
electronically storing in a computer readable medium said received financial market transaction data;

constructing an inhomogeneous time series z that corresponds to said received financial market transaction data;

constructing a complex iterated exponential moving average operator $\text{EMA}[\tau; z]$, with kernel ema ;

5 constructing a time-translation-invariant, causal operator $\Omega[z]$ that is a convolution operator with kernel ω and time range τ , and that is based on said complex iterated exponential moving average operator;

constructing a windowed Fourier transform WF that depends on said EMA operator;

electronically calculating values of one or more predictive factors relating to said time series z , wherein said one or more predictive factors depend on said windowed Fourier transform; and

electronically storing in a computer readable medium said calculated values of one or more predictive factors.

15 21. The method of claim 20 wherein said complex iterated exponential moving average operator EMA has a kernel ema of the form:

$$\text{ema}[\zeta, n](t) = \frac{1}{(n-1)!} \left(\frac{t}{\tau} \right)^{n-1} \frac{e^{-\zeta t}}{\tau}, \text{ where } \zeta \in \mathbb{C}, \text{ with } \zeta = \frac{1}{\tau} (1 + ik).$$

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22. The method of claim 20 wherein EMA is computed using the iterative computational formula:

$$\text{EMA}[\zeta; z](t_n) = \mu \text{EMA}[\zeta; z](t_{n-1}) + z_{n-1} \frac{\nu - \mu}{1 + ik} + z_n \frac{1 - \nu}{1 + ik}, \text{ with}$$

$$\alpha = \zeta(t_n - t_{n-1})$$

$$\mu = e^{-\alpha}$$

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where ν depends on a chosen interpolation scheme.

23. The method of claim 20 wherein said windowed Fourier transform has a kernel wf of the form:

$$\text{wf}[\tau, k, n](t) = \frac{1}{n} \sum_{j=1}^n \text{ema}[\zeta, j](t).$$

24. The method of claim 23 wherein said ema is of the form:

$$5 \quad \text{ema}[\zeta, n](t) = \frac{1}{(n-1)!} \left(\frac{t}{\tau} \right)^{n-1} \frac{e^{-\zeta t}}{\tau}, \text{ where } \zeta \in \mathbb{C}, \text{ with } \zeta = \frac{1}{\tau} (1 + ik).$$

25. A method of obtaining predictive information for inhomogeneous time series, comprising the steps of:

electronically receiving time series data over an electronic network;

10 electronically storing in a computer-readable medium said received time series data;

constructing an inhomogeneous time series z that represents said time series data;

constructing an exponential moving average operator;

constructing an iterated exponential moving average operator based on said exponential moving average operator;

15 constructing a time-translation-invariant, causal operator $\Omega[z]$ that is a convolution operator with kernel ω and that is based on said iterated exponential moving average operator;

electronically calculating values of one or more predictive factors relating to said time series z , wherein said one or more predictive factors are defined in terms of said operator

20 $\Omega[z]$; and

electronically storing in a computer readable medium said calculated values of one or more predictive factors.